

1. Write the Schrodinger equation for **third order** approximation of perturbation theory.
2. Write the Schrodinger equation for **zero order** approximation of perturbation theory.
3. Can you prove the following expression (page 127): "In the first order approximation of λ coefficient a_n^1 must satisfy $a_n^1 + (a_n^1)^* = 0$ ".
4. Can you prove the following equation for **second order approximation** (page 129):

$$\sum_{k \neq n} |a_k^1|^2 + ((a_n^2)^* + a_n^2) = 0$$
5. Can you prove that for **harmonic oscillator in constant force field** (page 129) "...the first order energy correction is equal to zero $E_n^1 = H'_{nn} = 0$ ".

6. Why for the second-order energy correction of a harmonic oscillator in a constant force field (p. 129) we need to take into account only two terms of the sum $n, n + 1$ and $n, n-1$

$$E_n^2 = \sum_{k \neq n} \frac{|H'_{nk}|^2}{E_n^0 - E_k^0} = \frac{|H'_{n, n+1}|^2}{E_n^0 - E_{n+1}^0} + \frac{|H'_{n, n-1}|^2}{E_n^0 - E_{n-1}^0} = \frac{F^2}{\hbar \omega} (-|x_{n, n+1}|^2 + |x_{n, n-1}|^2) = -\frac{F^2}{2M\omega^2}.$$

7. Can you prove that for anharmonic oscillator the first order energy correction for cubic term must be equal zero (page 130)?