

1. Derive classical expressions for L_x, L_y, L_z projections for angular momentum vector.
2. Derive expressions for the projections of the angular momentum operator $\hat{L}_x = -i\hbar \left(y \frac{\partial}{\partial z} - z \frac{\partial}{\partial y} \right)$, $\hat{L}_y = -i\hbar \left(z \frac{\partial}{\partial x} - x \frac{\partial}{\partial z} \right)$, $\hat{L}_z = -i\hbar \left(x \frac{\partial}{\partial y} - y \frac{\partial}{\partial x} \right)$.
3. Derive the commutation relation for x and y projections of angular momentum operator $[\hat{L}_x, \hat{L}_y] = i\hbar \hat{L}_z$.
4. Is it possible to measure simultaneously the x and z projections of angular momentum? Why? Proof.
5. Is it possible to measure simultaneously the square of angular momentum and its z projection of angular momentum? Why? Proof.
6. Is it possible to measure simultaneously the square of angular momentum and its x projection? Why? Proof.
7. Is it possible to measure simultaneously the absolute value of angular momentum $|\vec{L}|$ and its x projection? Why? Proof.
8. Write an expression for the x, y and z projections of circular frequency operators $\hat{\omega}_x, \hat{\omega}_y, \hat{\omega}_z$ (The rotating body is a sphere with mass \mathbf{M} and radius \mathbf{R}).
9. How can the angle between the angular momentum vector and the z -axis be calculated in quantum mechanics? Calculate the allowed possible values of this angle for orbital quantum number $l=1$.
10. How in quantum mechanics can be calculated the angle between the angular momentum vector \vec{L} and the z -axis? Calculate the values of this angle for **orbital quantum number** $l=1$ and **magnetic quantum numbers** $m=-2$ and $+1$.
11. How to calculate in quantum mechanics the kinetic energy of a rotating body with the moment of inertia \mathbf{I} ? If the body is an electron moving around a nucleus in orbit with radius 10^{-10} m. Calculate the velocity of the electron in this orbit if the orbital quantum number $l=5$ (NB! Electron is a point particle).
12. How to calculate in quantum mechanics the kinetic energy of a rotating body with the moment of inertia \mathbf{I} ? If the body is an electron moving around a nucleus in orbit with radius 10^{-10} m. Calculate the minimum possible non-zero value of the velocity of the electron (NB! Electron is a point particle).