

60

4) No, it's only possible to measure 1 projection, while 2 others are arbitrary. It is an uncertainty principle consequence.

Proofs ?

2

$$17) \underline{M} = \hbar \sqrt{L(L+1)} \quad (1)$$

$$M_z = m \hbar$$

If we need the minimal possible angle between M and M<sub>z</sub>, then M<sub>z</sub> should be maximal, thus:

$$M_z = L \hbar$$

$$\cos \alpha = M_z / M = L / \sqrt{L(L+1)}$$

$$M_{\text{classical}} = I \omega = m \cdot 0.5 \cdot (r^2) \cdot 2 \pi \cdot 1 \text{ Hz} = \pi \cdot 10^{-12}$$

$$(1) \Rightarrow \sqrt{L(L+1)} = \pi \cdot 10^{-12} / \hbar$$

Because of the fact that L is going to be quite large we can round left side of expression:

$$L = \pi \cdot 10^{-12} / \hbar = 2,98 \cdot 10^{22}$$

$$\cos \alpha = L / \sqrt{L(L+1)} = 1 / \sqrt{1 + 1/L} \approx 1 \text{ (my calculator isn't capable enough)}$$

$$\alpha \approx 0^\circ$$

$\alpha \approx 0^\circ$  but  $>0$  This is what is important !!!

18

25) electron in hydrogen atom has energy:

$$E_n = -R \hbar / n^2, \quad R = 2,07 \cdot 10^{16} \text{ s}^{-1}$$

20

$$\text{In ground state } n = 1 \Rightarrow E_n = -R \hbar$$

To ionize an electron means to remove it from atom for an infinitely long distance, so

$$n = \infty,$$

$$E_n = -R \hbar / n^2 = 0$$

Energy required to ionize an electron from ground state:

$$A = E_1 - E_{\text{inf}} = R \hbar = 2,18 \cdot 10^{-18} \text{ J}$$

34) Pauli principle states that an atom can only have electrons with unique set of quantum numbers:

$n: 0, 1, 2, \dots$

$l: 0, 1, 2, \dots, n-1$

$m: -l, \dots, l$

$s: \pm 0.5$

20

Thus, electrons are divided into layers with different principal quantum number  $n$ :

K,  $n=1$ , 2 electrons

L,  $n=2$ , 8 electrons

M,  $n=3$ , 18 electrons

N,  $n=4$ , 32 electrons

...

And are also divided into groups with different orbital quantum numbers (s, p, d, f, ...)

N (natrium):  $1s^2 2s^2 2p^3$

Cl:  $1s^2 2s^2 2p^6 3s^2 3p^5$

K (kalium):  $1s^2 2s^2 2p^6 3s^2 3p^6 4s$

43 ?????